

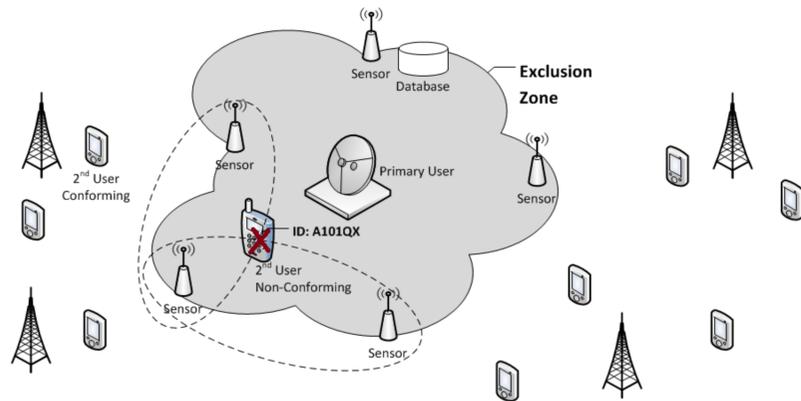
# Paving Way to Dynamic Spectrum Sharing: Understanding Spectrum Regulation and Enforcement Mechanics

2013

October 7 and 8  
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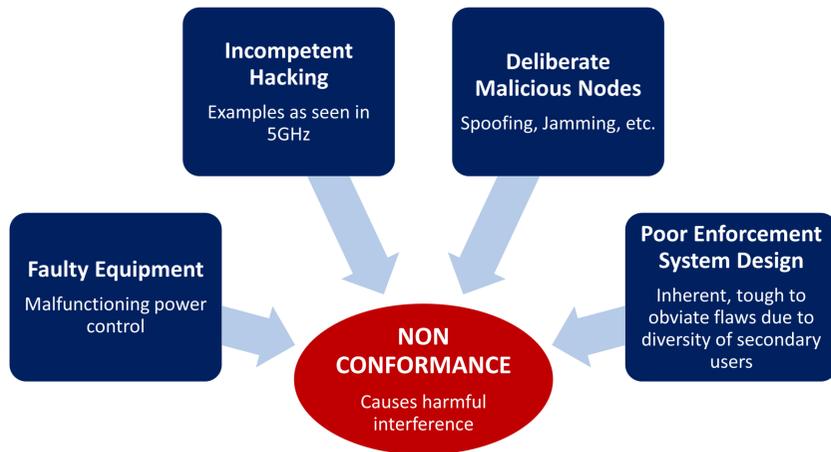
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## Spectrum Enforcement of DSA Radios

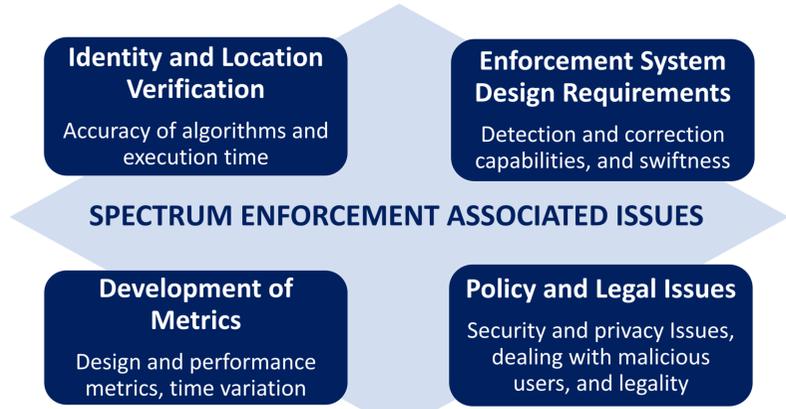


Can protection of incumbents from harmful interference be assured?

## What Causes Harmful Interference?

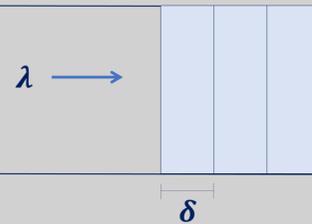


## Enforcement System Design Considerations



## Problem Formulation

### A Modified Queuing Problem



- What fraction of the unit time does it take to evict faulty users?
- Can probabilistic assurance be provided, given the following parameters?

### System Description

- Suspicious nodes are queued into the enforcement system for trial
- Enforcement system employs several identification and location verification algorithms to judge
- Depending on the node parameters, algorithm processing time varies

### Initial Assumptions

- Level of Interference is binary
- Time to resolve and interference index are the metrics used
- All “arrests” made are independent
- All faulty nodes are arrested
- Arrest rate,  $\lambda >$  Rate of faulty node occurrence,  $\rho$

$N$	Total number of nodes	$n_t$	Number of nodes in the queue at time instant $t$
$\lambda$	“Arrest” rate (Arrival rate)	$m_t$	Number of faulty nodes in the queue at time instant $t$
$p_T(\tau)$	PDF of algorithm processing time	$\beta$	Probability of missed detection
$\rho$	Rate of faulty node occurrence	$\delta$	Smallest time interval

Probability density function of  $n_t, m_t$  is the standard Poisson  

$$P_k = \frac{(\ell t)^k}{k!} \exp(-\ell t)$$
 where  $k, \ell = n_t, \lambda$  or  $m_t, \rho$  depending on the variable of interest

Algorithm processing time is a random variable assumed to be Gaussian  $\mathcal{N}(\mu, \sigma)$   
 Thus, the statistics of the problem depend on the independent RVs:  $n_t, m_t, \tau$

Average time to resolution is,  

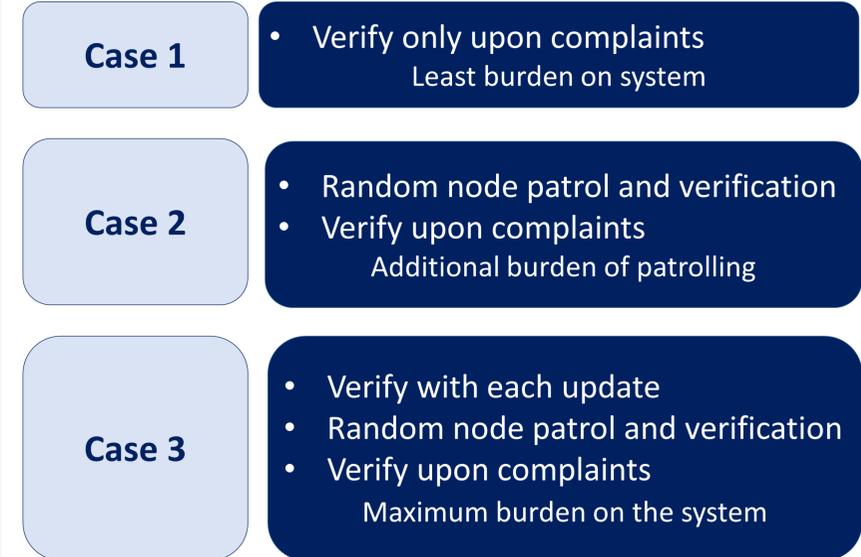
$$T_{avg} = \frac{(\lambda + \rho)\mu}{2} (1 - \beta)$$
 Variance of time to resolution is,  

$$T_{var} = \frac{(\lambda + \rho)\sigma}{2} (1 - \beta)$$

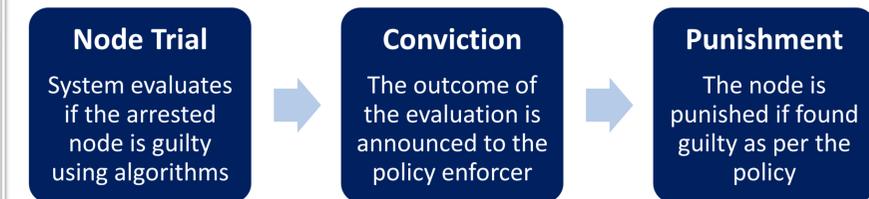
Interference Index is a proposed metric to evaluate the mean success of the enforcement system. It gives a measure of the interference mitigated  

$$I_{ind} = \frac{T_{avg} - \beta}{\lambda + \rho}$$

## Enforcement System Strategies



## Spectrum Enforcement Framework



## Time to Mitigate Harmful Interference



- Delay in the queue is dependent on system processing time
- Speed of algorithms decides the system processing time
- What are the constraints on system processing time for speedy enforcement?

## The Path Ahead

- Derive confidence intervals and enhanced feasibility metrics based on the distributions
- Relax the several assumptions made
  - Arrests need not be independent
  - Co-operative misbehavior frameworks
  - Block arrivals instead of individual node arrival
- Extensive simulations to validate the theoretical models