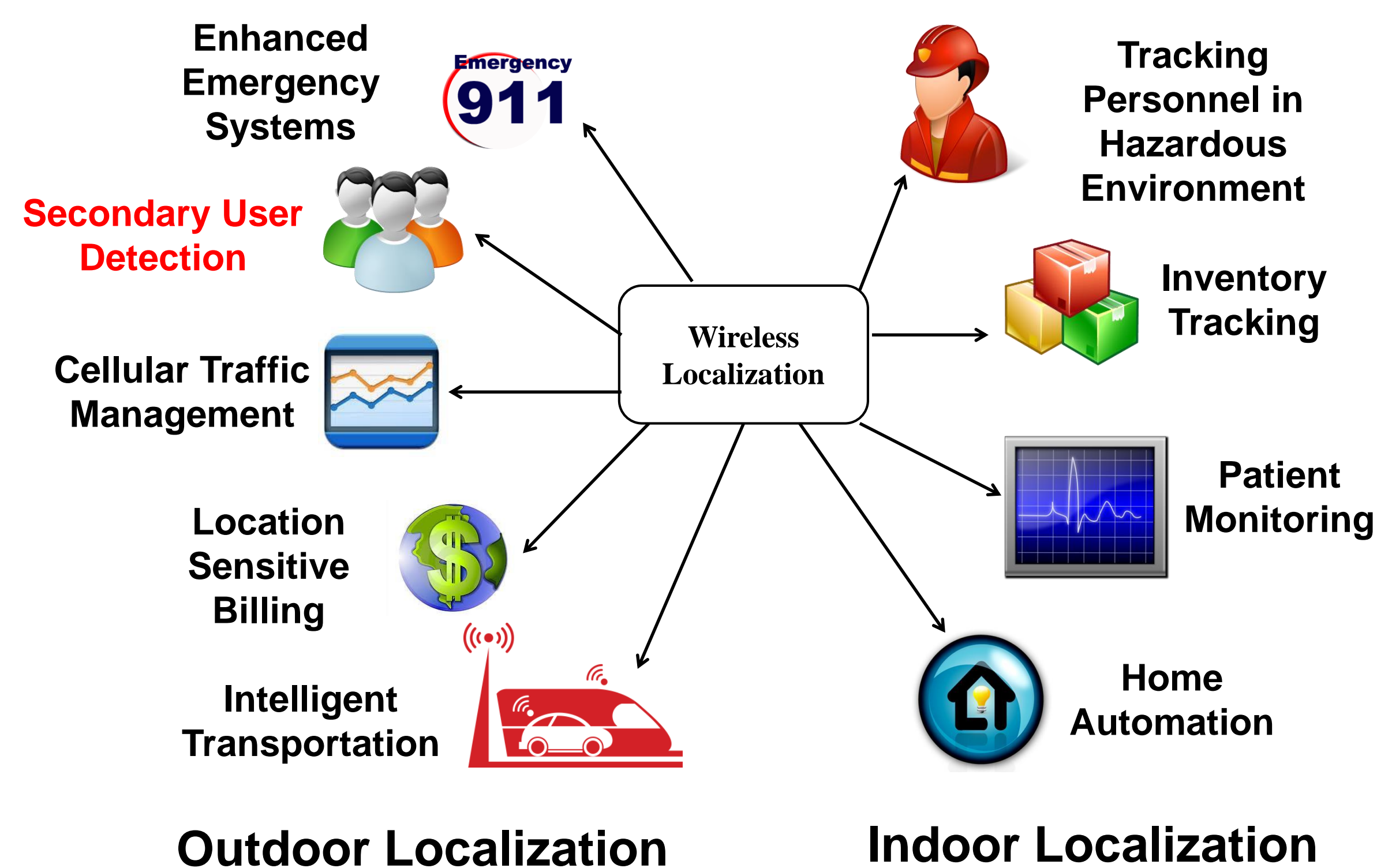


# Localization Aspects of Enforcing Spectrum Rights

2013

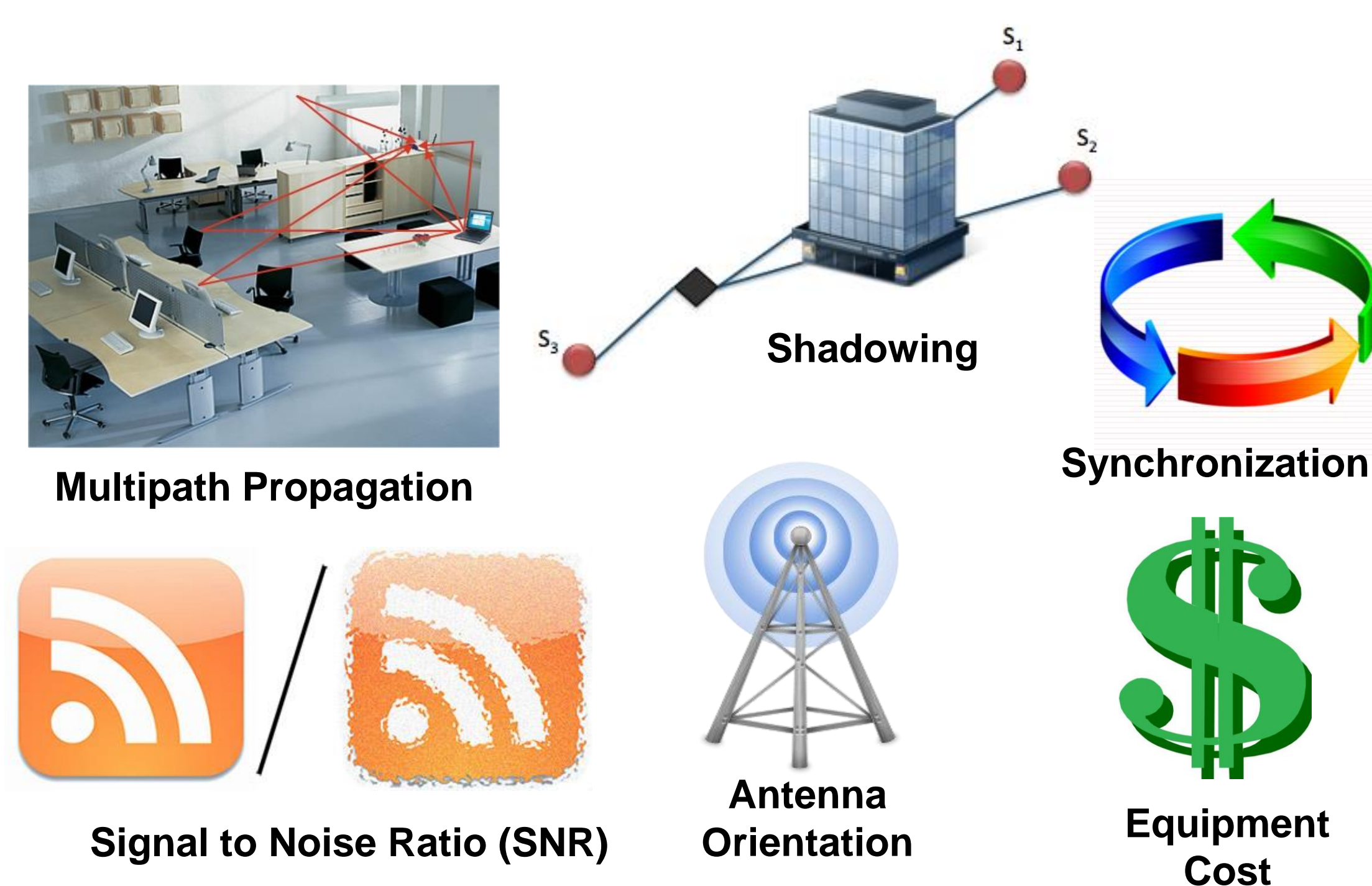
October 7 and 8  
NSF EARS WorkshopPIs: Jeffrey H. Reed, Michael Marcus, and A. A. (Louis) Beex  
Graduate Student: Tamoghna Roy

## WIRELESS LOCALIZATION: APPLICATIONS



Secondary User Detection : Intrinsic part of the Enforcement scheme

## WIRELESS LOCALIZATION: CHALLENGES



## SUMMARY OF METHODS

|                                      | Time of Arrival (TOA) | Angle of Arrival (AOA) | Received Signal Strength (RSS)         | Channel Impulse Response (CIR)                   |
|--------------------------------------|-----------------------|------------------------|--|--|
| Susceptibility to Multipath and NLOS | YES                   | YES                    | NO<br>(provided the model is accurate) | NO<br>(provided the database is extensive)       |
| Robustness to Noise                  | YES                   | YES                    | NO                                     | YES  |
| Low Cost                             | YES                   | NO                     | YES                                    | NO<br>(cost of maintaining the database is high) |
| Synchronization Required             | YES                   | NO                     | NO                                     | NO   |
| Database                             | NO                    | NO                     | NO                                     | YES  |

■ Desired    ■ Undesired

## RSS BASED METHODS

### 1. Received Signal Strength (RSS)

- **Log-Distance Relationship** :  $P(d_k) = P(d_0) - 10\alpha \log_{10} \left( \frac{d_k}{d_0} \right)$
- **Advantage**: Cost Effective Solution
- **Drawback**:  $P(d_0)$  needs to be calibrated and hence less robust.

### 2. Differential Received Signal Strength (DRSS)

- **Pairwise difference of the RSS values**:  $L(d_i, d_j) = 10\alpha \log_{10} \left( \frac{d_j}{d_i} \right)$
- **Advantage**: More robust as no calibration is required

### 3. Weighted Differential Received Signal Strength (WDRSS)

- Each pairwise difference is assigned a weight
- **Advantage**: Weights provide flexibility while retaining robustness

## SIMULATION EXAMPLE

**Simulation Environment**: 1000m by 1000m area with varying degrees of spatial correlation.

**Log-Distance Model with spatial Correlation**:

1. **RSS**:  $L(d_k) = P(d_0) - 10\alpha \log_{10} \left( \frac{d_k}{d_0} \right) + x_k$ , where  $X_k \sim N(0, \sigma_s^2)$
2. **DRSS**:  $L(d_i, d_j) = 10\alpha \log_{10} \left( \frac{d_j}{d_i} \right) + \Delta x_{ij}$ , where  $\Delta X_{ij} \sim N(0, 2(1 - \rho_{ij})\sigma_s^2)$ ,  $\rho$  spatial correlation coefficient

### Preliminary Results

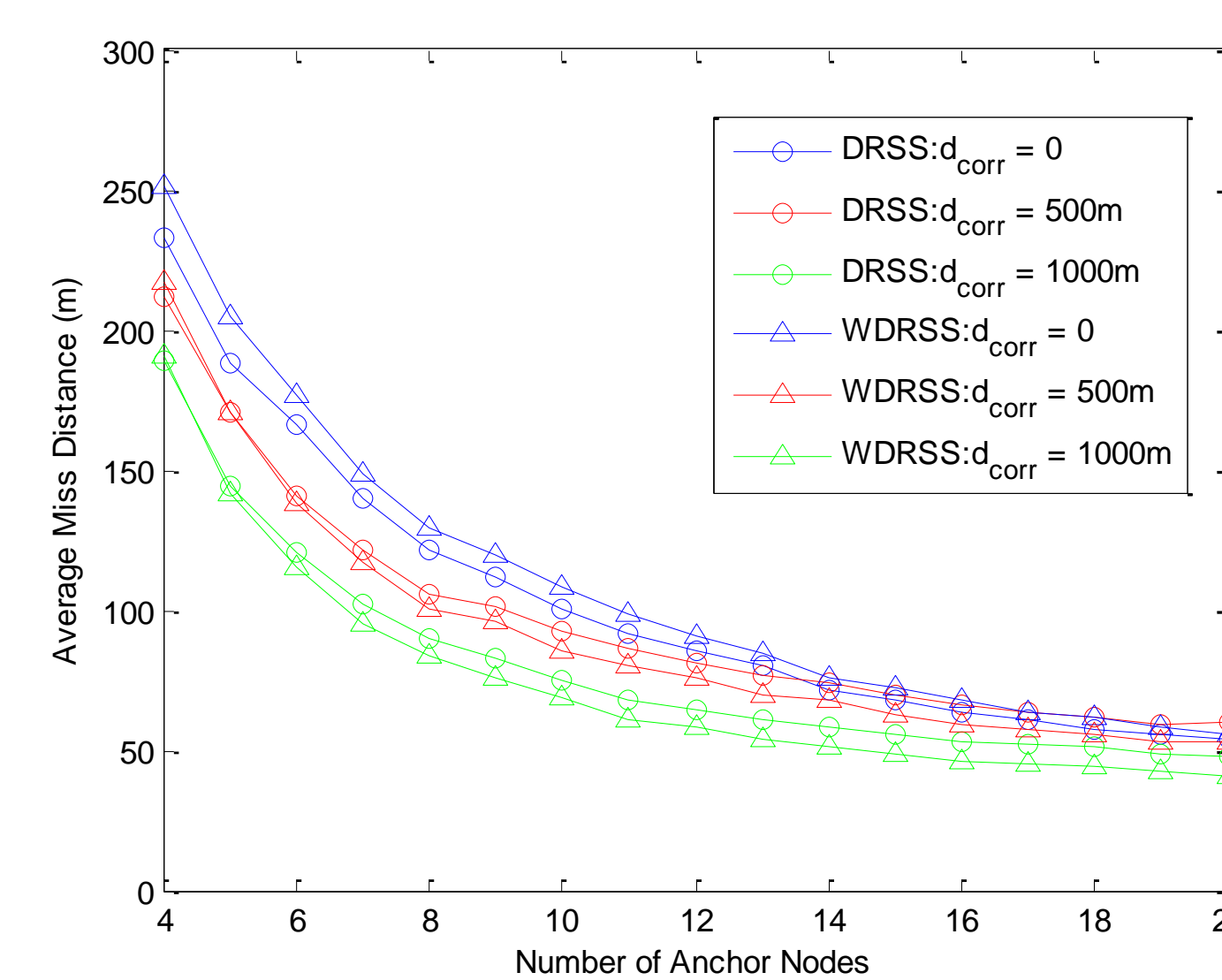
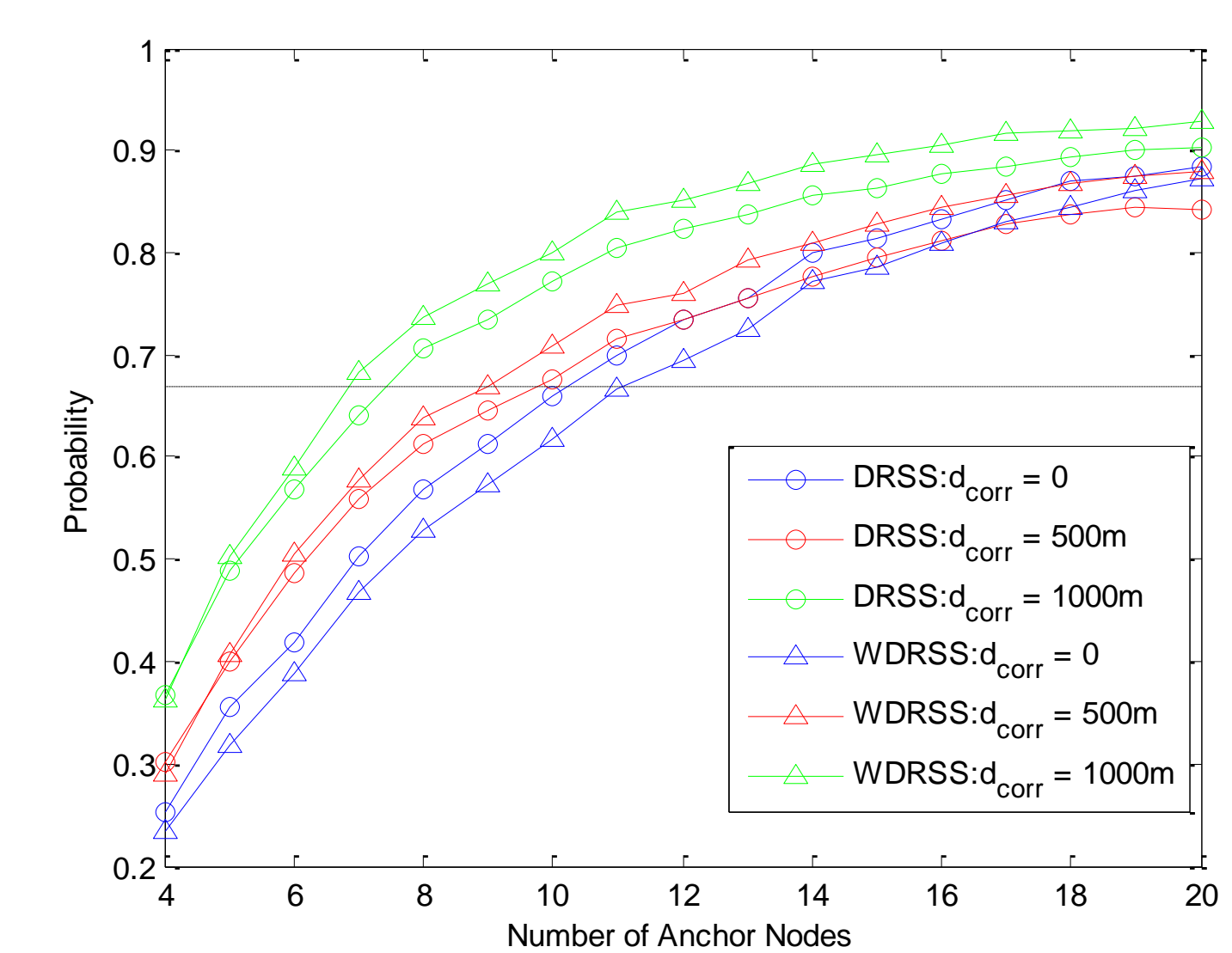
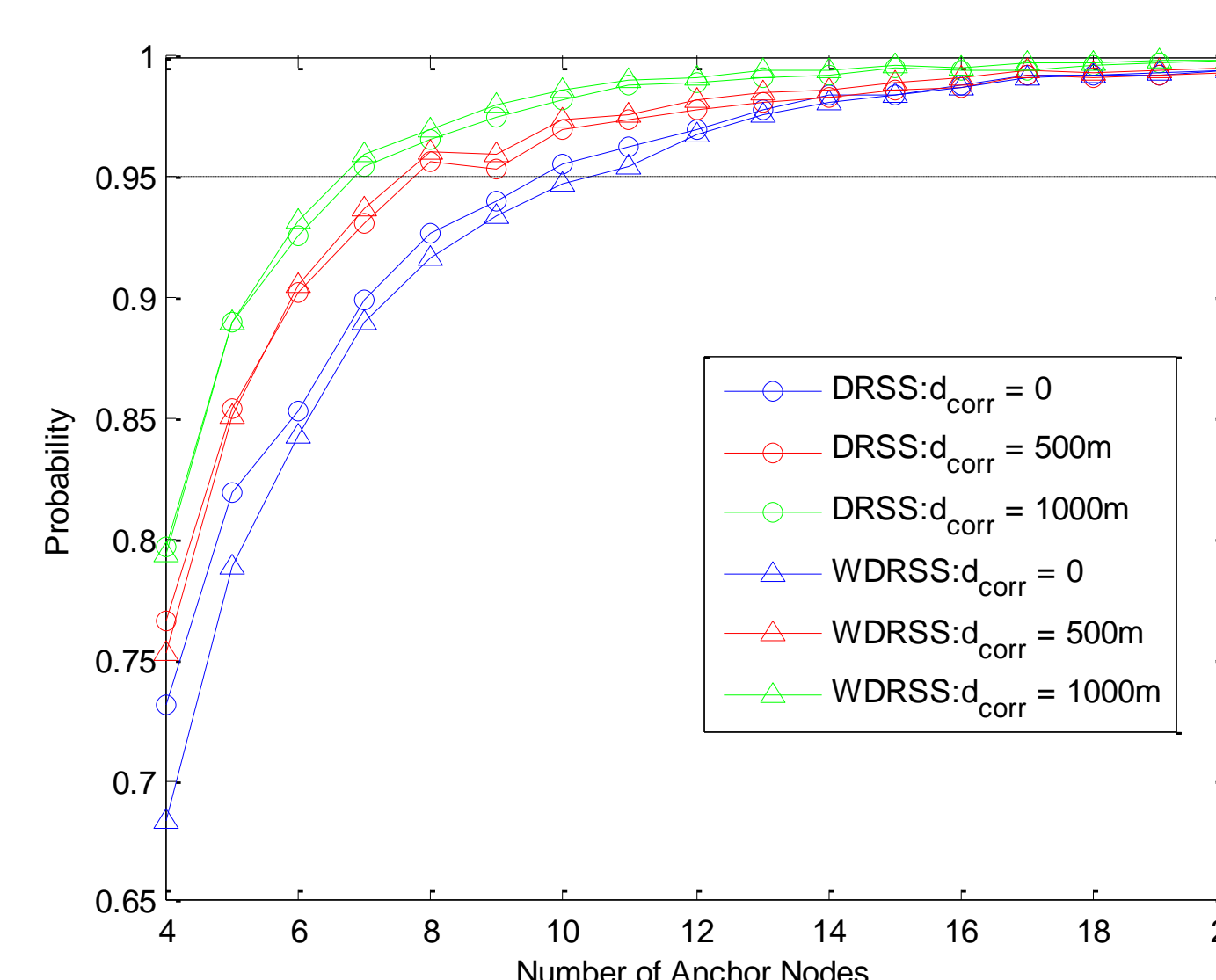


Figure 1: Average Miss Distance (AMD)

Figure 2:  $P(\text{AMD} \leq 100\text{m})$ Figure 3:  $P(\text{AMD} \leq 300\text{m})$ 

## DISCUSSION

- In a more spatially correlated environment the performance of both DRSS and WDRSS improves.
- Figures 2 and 3 give an idea of the minimum number of sensors (anchor nodes) required to meet the FCC E-911 specifications.
- In the future, we want to investigate the performance of different methods under different simulation environments to learn which one is optimum under which conditions.